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# **Determination of Physical Parameters of Drift Transistors Having a Diffused Collector Junction**

by

**A. R. Boothroyd**

Series No. 60, Issue No. 391

AF 49(638)-1043

August 11, 1961

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**DETERMINATION OF PHYSICAL PARAMETERS OF DRIFT  
TRANSISTORS HAVING A DIFFUSED COLLECTOR JUNCTION**

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**Air Force Office of Scientific Research  
of the Air Research and Development Command;  
Department of the Navy, Office of Naval Research;  
and Department of the Army  
Contract No. AF 49(638)-1043**

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## LIST OF PRINCIPAL SYMBOLS

$N$	impurity density in the base
$L$	critical length defining an exponential distribution of $N$
$D$	diffusion constant of minority carriers in the base
$m$	electric field parameter $= \Delta V / (kT/q) \doteq w / L$
$w$	electrical base width
$d$	collector depletion layer width
$A_e$	emitter area
$\kappa$	absolute permittivity of base material
$\psi_{eo}$	contact potential of emitter junction
$n_i$	intrinsic hole and electron density
$w_b$	distance between collector and emitter junction transition points
$\tau$	intrinsic base transit time
$\tau'$	"effective transit time" $= 1 / (2\pi f_T)$

## SUMMARY

A procedure for the determination of physical parameters of drift transistors with a diffused collector junction has been developed on the assumption of a device model with exponential base grading. Only relatively low-frequency measurements are involved. Studies have been made of a double-diffused silicon mesa unit (Fairchild 2N696) and the results obtained suggest that the theory used may be adequate for practical application, despite discrepancies between the assumed model and the actual device. Good correlation between certain known design values of physical parameters of the device, and the values deduced from measurements, has been obtained. More investigation is necessary, however, in order to establish the conditions of validity, accuracy and possible need for further elaboration of the approach presented.

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## I. INTRODUCTION

It has been found possible to derive a considerable amount of physical data for drift transistors of alloy-junction type by measuring the dependence of effective transit time (i. e.,  $1/\omega_T$ ) and collector capacitance on collector voltage<sup>1, 2</sup>. Assuming a specific form of impurity density distribution in the base--viz. exponential or complementary error function--such measurements lead to the derivation of base width, field parameter  $m = \Delta Vq/kT$ , collector depletion layer width, emitter area, impurity density as a function of distance and other related properties. The physical properties exploited in these derivations are illustrated in Figure 1a: a change in collector voltage causes change in both the minority carrier charge  $Q$  in the base region and the space charge in the collector depletion layer, resulting in corresponding changes in base transit time  $\tau = Q/I_e$  and collector capacitance  $C_c$ . In the case of the alloy junction device, as shown, the changes in base width and depletion layer thickness are equal and opposite, a property that leads to relatively simple relationships between changes in  $\tau$  and  $C_c$ . Specifically, for an alloy junction transistor with base impurity density distribution of the form

$$N = N_0 e^{-x/L}, \quad (1)$$

it may be shown that

$$L \approx \sqrt{\frac{D (\tau_1 - \tau_2)}{\ln \left( \frac{V_{c1} C_{c1}}{V_{c2} C_{c2}} \right)}} \quad (2)$$

where  $\tau_1$ ,  $C_{c1}$  and  $\tau_2$ ,  $C_{c2}$  are measured at collector voltages  $V_{c1}$  and  $V_{c2}$ , respectively. Then, for given  $V_c$ ,

$$\tau \approx \frac{L^2}{D} (m - 1) \quad (3)$$

so that

if  $m \geq 3$

$$m \approx \frac{\tau D}{L^2} + 1 \quad (4)$$

and base width  $w$  is

$$w \approx m L \quad (5)$$

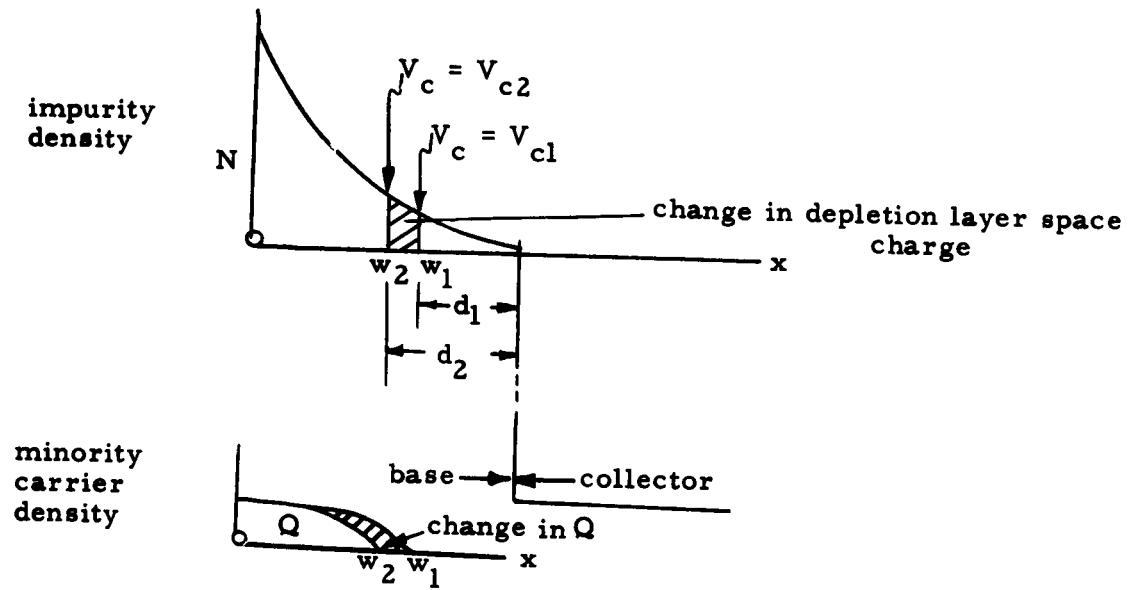
Having determined the above parameters, the values of impurity density  $N_0$  and emitter area follow from measurements of the dependence of emitter depletion capacitance on reverse bias voltage and the d. c.

$I_c \sim V_{eb}$  characteristic of the device with emitter forward and collector reverse biased.

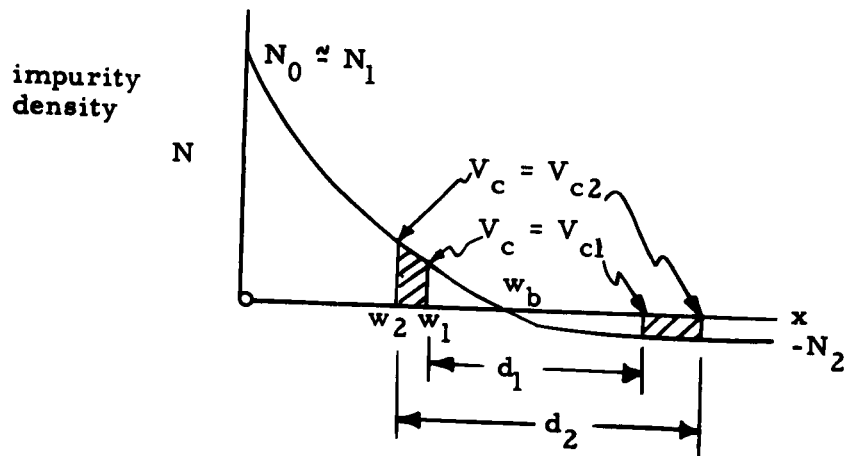
The above process of parameter evaluation is applicable only for a device with a step collector junction and exponential base impurity grading. If the collector junction is graded, as when formed by a diffusion process (e. g., mesa device), changes in base width and collector depletion layer width resulting from collector voltage change are not equal and opposite, as illustrated in Figure 1b: equation (2) does not apply in such a situation. This report presents a procedure for the derivation of physical parameters of drift transistors of diffused collector junction type, following along the lines outlined above for the step junction device. Exponential base grading is assumed, so that equations (3) - (5) apply. Alternatively, a complementary error function distribution of impurity density may be considered and similar relationships derived, equations (3) and (4) still being valid<sup>2</sup>. The most appropriate form of base grading needs to be established for the class of device concerned, possibly using the approach presented in reference 2; this matter is not pursued, however, in the present report.

## II. THEORETICAL BASIS OF THE METHOD OF PHYSICAL PARAMETER DERIVATION

In order to keep the analysis within reasonable bounds of simplicity it is necessary to represent the transistor by a somewhat idealized model, as follows. The device cross-section of Figure 2a is assumed, for a mesa or planar diffused base device of linear or circular geometry. All injected minority carriers comprising collector current are supposed to flow directly from emitter to collector within the emitter area  $A_e$ , without side effects.

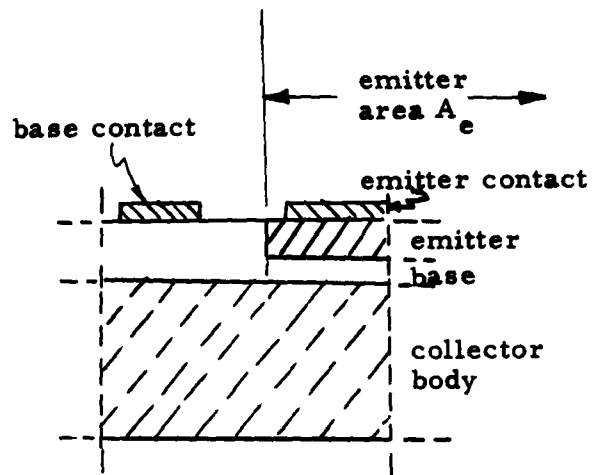


a) Step junction collector  $\Delta w = - \Delta d$

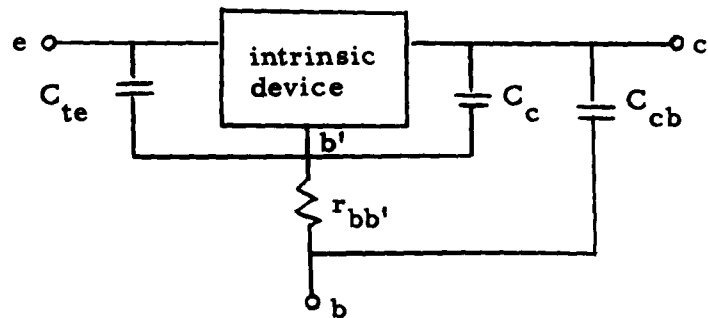


b) Diffused junction collector  $\Delta w \neq - \Delta d$

Figure 1. Step and Graded Collector Junctions



a) Assumed device cross-section



b) Assumed form of equivalent circuit (representation of collector body resistance omitted)

Figure 2. Device Assumptions

The effective base region is thus of area  $A_e$  and width  $w$ , and is regarded as obeying ideal one-dimensional theory. The complete device is considered to be represented by the equivalent circuit of Figure 2b in which  $C_c$  is the part of the total collector depletion capacitance opposite the emitter area  $A_e$ .

Further assumptions are that the base impurity density is (see Figure 1b) of the form

$$N(x) = N_1 e^{-x/L} - N_2, \quad (6)$$

so defining the graded collector junction transition point at

$$x = w_b = L \ln (N_1/N_2), \quad (7)$$

and that the emitter junction is either of step or very abrupt graded transition.

## II.1 Evaluation of the Basic Parameters $L$ , $m$ and $w$

The property utilized as the starting point in the determination of physical parameters is that the total depletion layer space charge is zero. Thus assuming complete depletion of impurities within depletion layer thickness  $d$ , and zero depletion elsewhere,

$$\int_w^{w+d} N(x) dx = 0 \quad (8)$$

giving the relationship

$$e^{w/L} = \frac{N_1}{N_2} \cdot \frac{L}{d} \left( 1 - e^{-d/L} \right) = e^m \quad (9)$$

Taking now two values  $V_{c1}$ ,  $V_{c2}$  of collector reverse voltage,

$$\begin{aligned} (w_1 - w_2)/L &= e^{m_1 - m_2} = \frac{d_2}{d_1} \cdot \left( \frac{1 - e^{-d_1/L}}{1 - e^{-d_2/L}} \right) \\ &= \frac{d_2}{d_1} \cdot \frac{1}{F} \end{aligned} \quad (10)$$

Now if  $d_1, d_2 \gg L$ ,  $F \approx 1$  and

$$e^{m_1 - m_2} \approx \frac{d_2}{d_1} = \frac{C_{c1}}{C_{c2}} \quad (11)$$

The assumption that  $\frac{d}{L} \gg 1$  will be made at this stage, but is not essential; if this condition is not obeyed the effect of the factor  $F$  may be included, as shown later. It should be noted that  $d/L$  does not need to be very large for  $F \approx 1$  because of the exponentials involved.

Writing  $m$  in terms of base transit time  $\tau$  from equation (3), one gets

$$\tau_1 - \tau_2 \approx \frac{L^2}{D} \cdot \ln (C_{c1}/C_{c2}) \quad (12)$$

where  $\tau_1$ ,  $C_{c1}$  and  $\tau_2$ ,  $C_{c2}$  are for collector voltages  $V_{c1}$  and  $V_{c2}$ , respectively. If now  $V_{c2}$  is fixed and  $V_{c1}$  varied, plotting  $\tau_1 - \tau_2$  against  $\ln (C_{c1}/C_{c2})$  should give a straight line, so verifying applicability of the theory for a given device and yielding the value of  $L$  from the slope of the line. Alternatively, for two collector voltages,

$$L \approx \sqrt{\frac{D (\tau_1 - \tau_2)}{\ln (C_{c1}/C_{c2})}} \quad (13)$$

If  $d/L \not\gg 1$ , then from equation (10)

$$L = \sqrt{\frac{D (\tau_1 - \tau_2)}{\ln (C_{c1}/F C_{c2})}} \quad (14)$$

where  $F$  involves knowledge of  $L$ ,  $d_1$  and  $d_2$ . Equation (14) may be solved for  $L$  by iteration if  $d$  is separately determined, as discussed below.

Having evaluated the critical length  $L$ ,  $m$  and  $w$  follow from equations (4) and (5), repeated here:

$$\left. \begin{aligned} m &= \frac{\tau D}{L^2} + 1 \\ w &= m L \end{aligned} \right\} \quad (15)$$

## II. 2 Evaluation of Other Parameters

The emitter area  $A_e$ , collector depletion layer width  $d$  and impurity densities  $N_1$ ,  $N_2$  may be evaluated if additional measurements are carried out.

For a step emitter junction of an n-p-n device, the depletion capacitance

$$C_{te} \approx A_e \left[ \frac{q K N_1}{2(\psi_e)} \right]^{1/2} \quad (16)$$

where

$$\psi_e = \psi_{eo} + V_{eb}$$

and the impurity density in the emitter depletion layer region of base material  $\propto N_1$ . Plotting  $1/C_{te}^2$  against reverse  $V_{eb}$ , a straight line of slope  $K_1 = 2/(q K N_1 A_e^2)$  results for such a junction from which the value of  $N_1 A_e^2$  is known; viz.

$$N_1 A_e^2 = 2/(q K K_1) \quad (17)$$

For small emitter current, such that true low level injection conditions obtain, and with the collector junction reverse biased,

$$I_c \approx A_e \frac{n_i^2}{N_1} \cdot q \frac{D}{L} e^{-qV_{eb}/kT} + I_o \quad (18)$$

for an n-p-n device. Voltage drop across  $r_{bb}$ , is assumed to be negligible so that  $V_{eb}$  is the voltage applied across the emitter junction. Plotting  $I_c$  against  $\exp(-qV_{eb}/kT)$  gives a straight line of slope  $K_2$  where

$$\frac{A_e}{N_1} = K_2 \cdot \frac{L}{n_i^2 q D} \quad (18)$$

Hence, from equations (17) and (18),

$$A_e = \left[ \frac{2 K_2 L}{q^2 K K_1 n_i^2 D} \right]^{1/3} \quad (19)$$

$$N_1 = \frac{A_e n_i^2 q D}{K_2 L} \quad (20)$$

$N_2$  follows from equation (9), viz.

$$N_2 = N_1 \cdot \frac{L}{d} \left( 1 - e^{-d/L} \right) e^{-m}, \quad (21)$$

provided that  $d$  is known. The distance  $w_b$  between emitter and collector junctions is also defined by the ratio  $N_1/N_2$  as in equation (7).

Knowledge of the "inner" collector capacitance  $C_c$  allows the value of  $d$  to be calculated, assuming this capacitance to represent area  $A_e$  of the collector depletion layer, since then

$$C_c = \frac{K A_e}{d} \quad (22)$$

Measurement of  $r_{bb}$ , and the product  $r_{bb} C_c$  give the value of  $C_c$ .

### II.3 Iteration

After carrying through the above sequence of calculations based on the condition  $F \approx 1$ , it is necessary to verify that this assumption is valid. If  $d/L$  is not sufficiently large for  $F \approx 1$ , as may be the case for a practical device, the value of  $L$  may be determined by iteration. Using the  $F$  value calculated as above, equation (14) is used to obtain a modified value of  $L$ .  $A_e$  is then recalculated from equation (19),  $d$  from (22) and a new  $F$  value obtained. This process is iterated until a further step leads to no further change in  $L$ .



### III. MEASUREMENT TECHNIQUES

For the above process of parameter determination to be carried out, the following quantities need to be measured:

1. base transit time  $\tau$
2. collector capacitance ratio  $C_{c1}/C_{c2}$  for two collector voltages
3. emitter depletion capacitance  $C_{te}$
4.  $I_c \sim V_{eb}$  characteristic
5. extrinsic base resistance  $r_{bb'}$ .

#### III.1 Base Transit Time Measurements

It is required to determine  $\tau$  and also transit time differences for two collector reverse bias voltages; in the latter very small fractional differences are possibly involved. For this purpose the bridge arrangement of Figure 3 may be used.

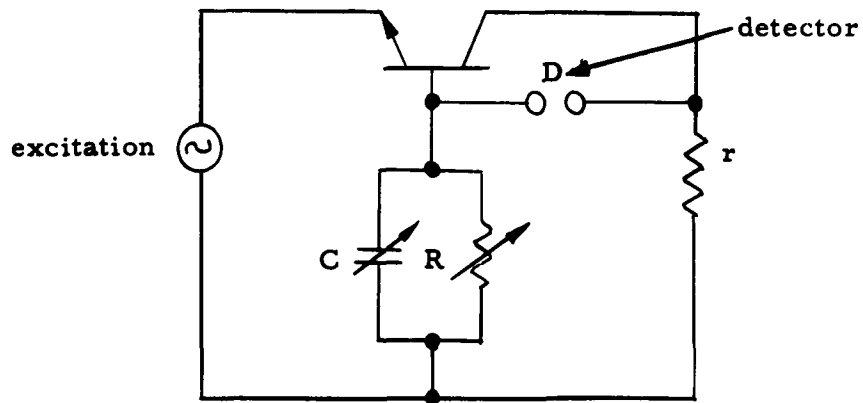


Figure 3. Arrangement of Bridge for Measurement of Transit Time

The bridge balance conditions are as follows: with R, C adjusted for null indication by the detector the transistor is operating with collector effectively shorted to base; thus

$$\frac{i_c}{i_b} = \beta = \frac{R}{r(1 + j\omega CR)} = \frac{\beta_o}{1 + j\omega/\omega_\beta} \quad (23)$$

so that

$$\left. \begin{aligned} \beta_o &= R/r \\ \omega_\beta &= 1/CR \\ \text{and } 1/\omega_T &= Cr = \tau' \end{aligned} \right\} \quad \text{if } \beta_o \gg 1 \quad (24)$$

$$\text{Now } \tau' = \tau + C_{te} r_d^+ \quad (25)$$

where  $\tau$  is the base transit time  $Q/I_e$  and

$$r_d = kT/q I_e$$

Plotting  $\tau' = 1/\omega_T$  against  $1/I_e$  yields a straight line of slope  $C_{te} \cdot kT/q$ ; extrapolating to  $1/I_e = 0$  gives  $\tau$ .

The bridge is convenient for measuring transit time differences since

$$\tau_1 - \tau_2 = \tau_1' - \tau_2' = r(C_1 - C_2) \quad (26)$$

Details of the practical arrangement of the bridge used for the measurements reported in Section IV are given in Appendix I. A noteworthy feature is the incorporation of a variable capacitor of small range calibrated directly in terms of  $C_1 - C_2$  for facilitating transit time difference measurements.

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<sup>+</sup> Assuming collector capacitance effects to be negligible. Otherwise  $\tau' \approx \tau + (C_{te} + C_c + C_{cb}) r_d$  (25a) if effects of collector body resistance may be neglected (i.e., this resistance on  $I_e$  sufficiently small for "Miller effects" to be insignificant). Referring to Figure 2b, presence of  $r_{bb'}$  is ignored in arriving at equation (25a).

### III. 2 Measurement of Collector Capacitance Ratios

With a base cross-section as in Figure 2a, it would seem reasonable to employ the ratio of either  $C_c$  values, or of total collector capacitance

$$C_{ob} = C_c + C_{cb},$$

in equations (12) to (14), provided that stray capacitance external to the collector depletion layer is negligible. In cases where stray capacitance is an appreciable fraction of  $C_{ob}$ ,  $C_c$  ratios must be used.

In practice it is more convenient to evaluate  $C_{c1}/C_{c2}$  as the ratio of  $r_{bb}$ ,  $C_c$  products for the collector voltage concerned, this product being readily measurable. Perhaps the most satisfactory method of determining  $r_{bb}$ ,  $C_c$  is by means of the Turner bridge<sup>3</sup>. In the absence of such a bridge an alternative method is to use the Wayne Kerr admittance bridge in the manner of Figure 4.

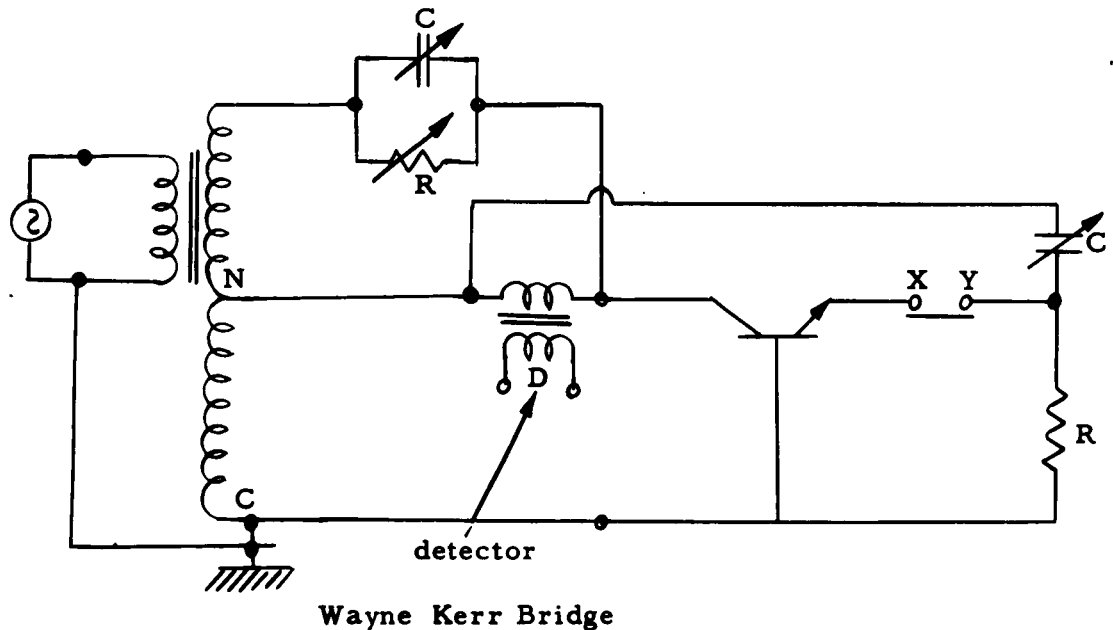


Figure 4. Arrangement for Measurement of  $r_{bb}$ ,  $C_c$  Using Wayne Kerr Bridge

With the points XY unconnected the bridge is balanced and  $C_{ob}$  (i. e., the common base parameter  $h_{22}$ ) measured. XY are then connected together and C is adjusted so that the bridge is again balanced; then

$$CR = r_{bb'} C_c \quad (27)$$

This method was used for the measurements of the next section, the practical arrangement of the bridge being as in Appendix II. The same jig was used for measurement of  $C_{te}$  as a function of reverse  $V_{eb'}$  by interchanging the emitter and collector connections.

### III.3 Measurement of $r_{bb'}$

There are many possible methods of measuring extrinsic base resistance values<sup>4</sup>, though the significance of the results obtained is often difficult to interpret in view of the distributed nature of extrinsic base region effects. For the present purpose it is preferable to use methods of measurement that are as closely as possible under the same conditions of operation of the transistor as employed when determining the product  $r_{bb'} C_c$ . Thus the transistor should be operated under the same d.c. bias conditions and at the same order of frequency, so that the flow of base current originates uniformly over the base cross-section as in the measurement of  $\tau'$ .

The method employed was to measure the base input  $y_{11}$  parameter with emitter common, at a frequency of the order of  $f_\beta$  (actually the same as for the  $\tau'$  measurement), and to evaluate  $r_{bb'}$  from a knowledge or estimate of all other relevant equivalent circuit parameters involved in this admittance. Thus, an estimate is made of  $C_{cb}$ , having measured  $C_{ob}$ ; then if effects of collector body resistance are negligible

$$\left. \begin{aligned} y_{11}' &= y_{11} - j\omega C_{cb} \\ 1/y_{11}' &= r_{bb'} + 1/y_{b'e} \end{aligned} \right\} \quad \text{where} \quad (28)$$

From measurements made at the same bias point and frequency with the bridge of Section III.1

$$y_{b'e} = (1 - a_o)/r_d + j\omega(\tau'/r_d - C_{cb})^+ \quad (29)$$

---

<sup>+</sup> See footnote on page 10 in regard to the approximation involved in this expression.

with appropriate choice of frequency the difference of real parts of  $1/y_{11}'$  and  $1/y_{b'e}$  gives  $r_{bb'}$  with reasonable accuracy. Having carried through the full procedure of calculation of Section II, the initial estimate of  $C_{cb}$  may be checked and if necessary corrected.

#### IV. PRACTICAL RESULTS

The measurements outlined in the previous section have been carried out for a variety of transistors of diffused base type having  $f_T$  ranging between 50 mc/s and 700 mc/s; the results obtained indicate that the measurement techniques described are suitable for the practical application of the parameter derivation process. For detailed study, an n-p-n silicon mesa transistor, Fairchild Type 2N696, was chosen, the selected device having conveniently low  $f_T$ . Certain physical data was available for this device with which derived parameters could be compared. The results reported in the present section are restricted to the study of this single device sample and should be regarded as a test of the feasibility of the procedure of parameter evaluation, rather than an exhaustive assessment of its applicability and accuracy.

##### IV.1 The Basic Measurements

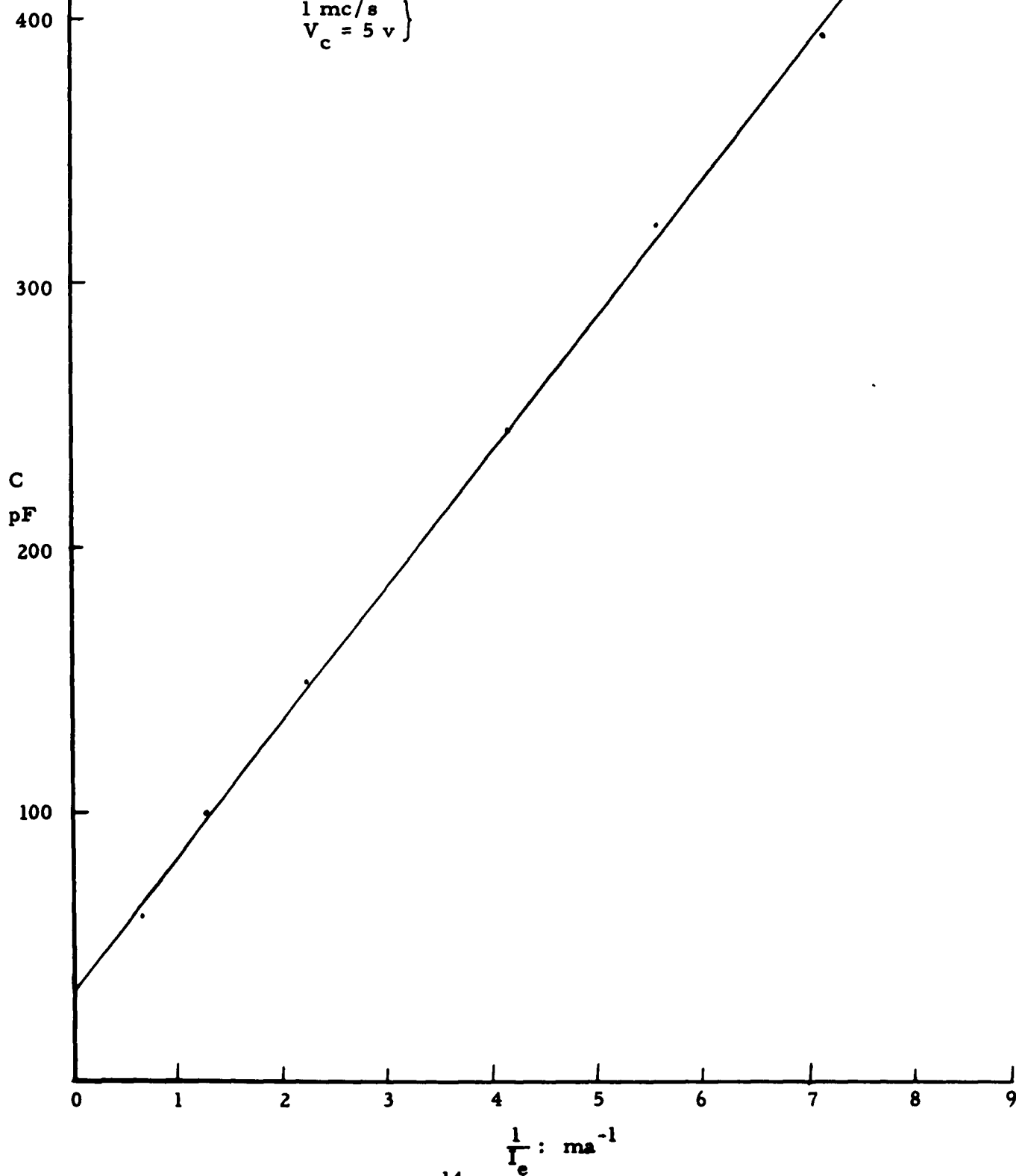
The theory of Section II assumes an idealized device with exponential base grading; although the grading for the type 2N696 undoubtedly deviates from this ideal (particularly near the emitter), the theory is applied in the following, the transistor being regarded as represented by an "exponential model". The basic measurements necessary are of  $\tau' (= 1/\omega_T)$  as a function of emitter current at constant collector voltage, and of change of transit time  $\tau$  and fractional collector capacitance  $C_c$  with change of collector voltage at constant emitter current. The results of these measurements, carried out at 1 mc/s, are given in Figures 5 through 7, respectively. Parameters are evaluated for  $V_c = 5$  v,  $I_e = -0.2$  ma.

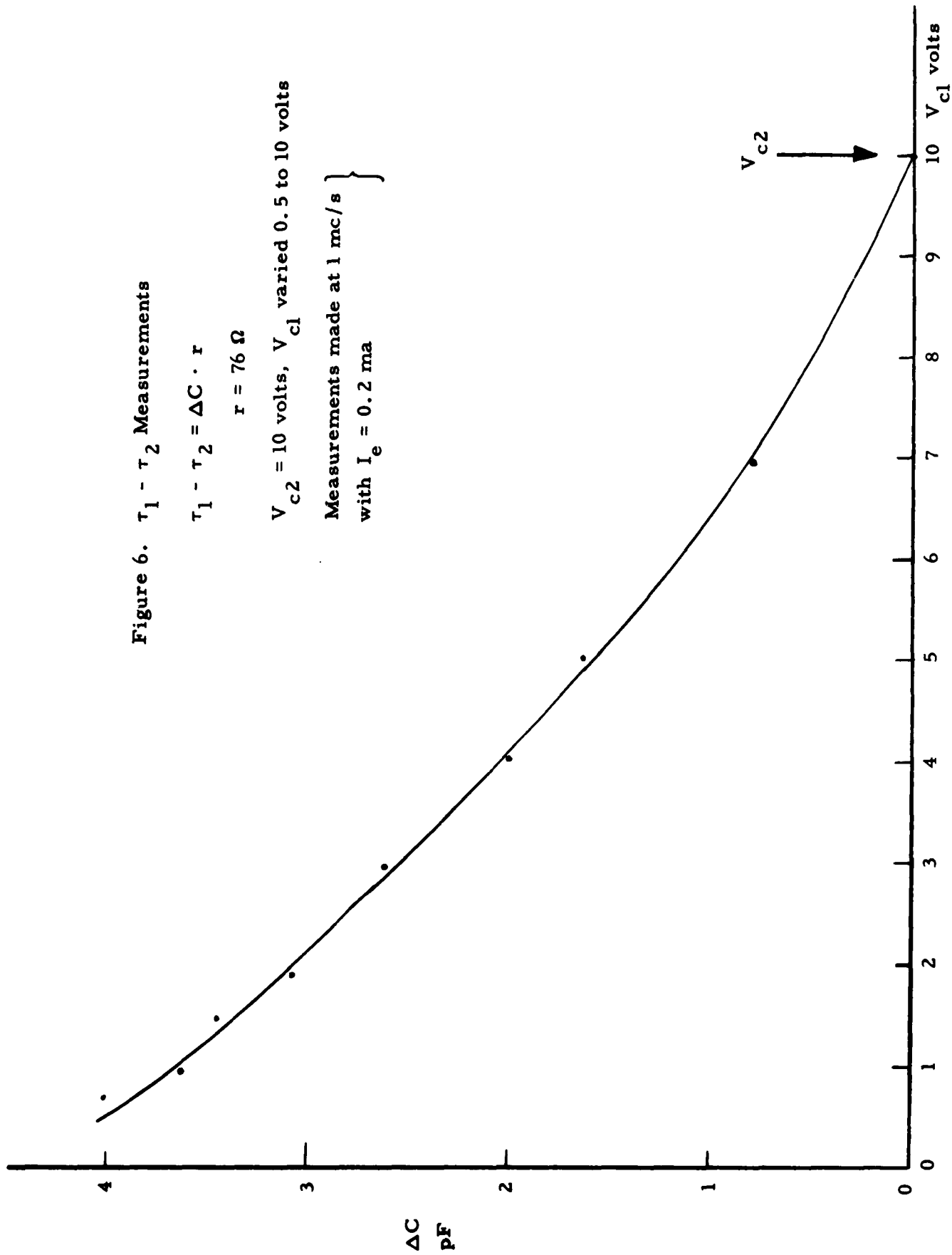
Figure 5. Plot of Effective Transit Time  $\tau'$   
Against  $1/I_e$

$$\tau' = Cr \text{ where } r = 76 \Omega$$

Measurements made at

$$\left. \begin{array}{l} 1 \text{ mc/s} \\ V_c = 5 \text{ v} \end{array} \right\}$$





$\Delta C$   
pF

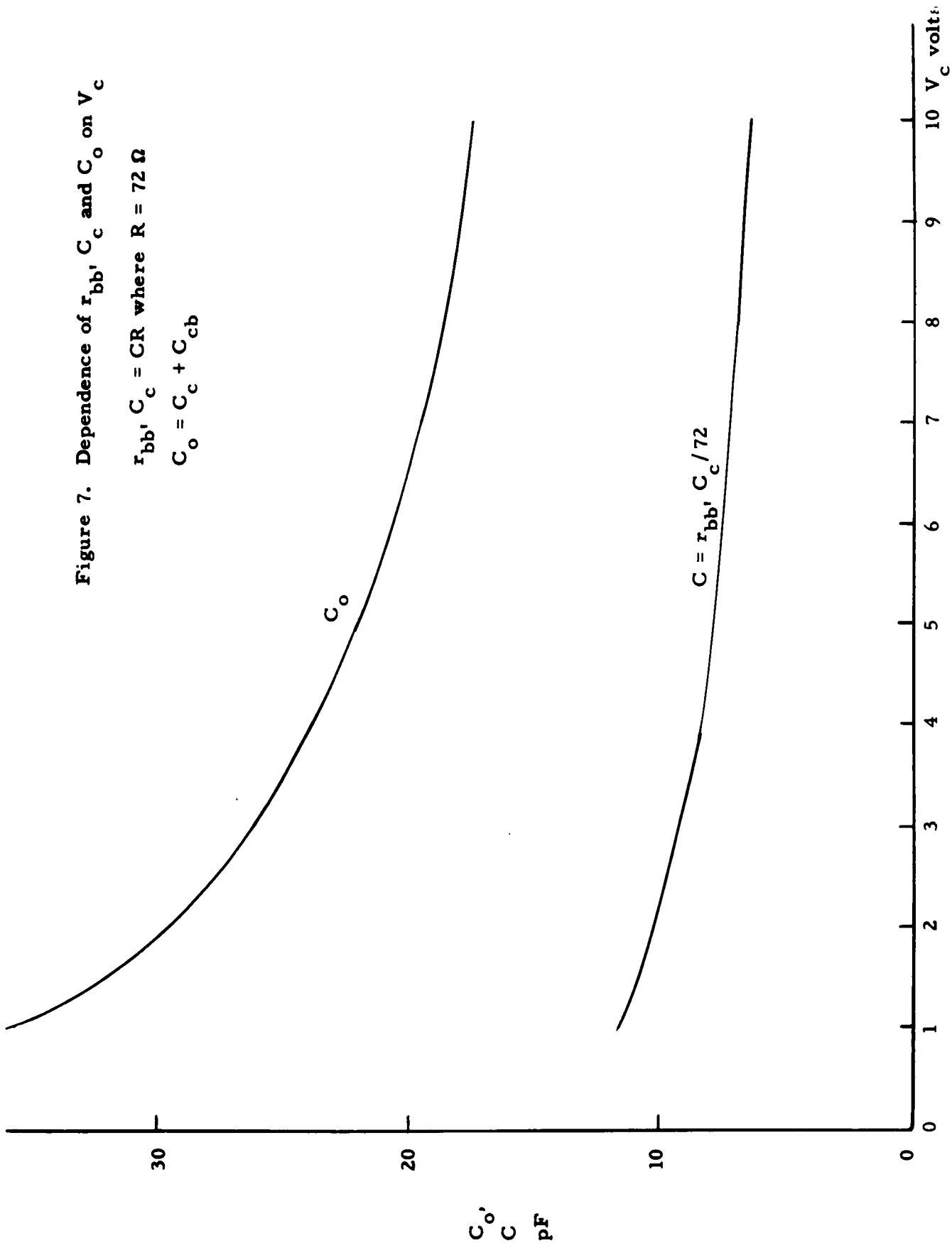


Figure 7. Dependence of  $r_{bb'}$ ,  $C_c$  and  $C_o$  on  $V_c$

$$r_{bb'}, C_c = CR \text{ where } R = 72 \Omega$$

$$C_o = C_c + C_{cb}$$



From the plot of  $\tau'$  against  $1/I_e$  in Figure 5 one obtains:

$$\tau = 2.36 \times 10^{-9} \text{ secs}$$

$$f_{\tau} = 1/2\pi \tau = 67.5 \text{ mc/s}$$

and  $C_{te} + C_{ob} = 150 \text{ pF}$

from the slope of the line. Also, for  $I_e = -5.0 \text{ ma}$ ,  $V_c = 5 \text{ v}$

$$\tau' = 3.2 \times 10^{-9} \text{ secs}$$

$$f_T = 1/2\pi \tau' = 50 \text{ mc/s}$$

In Figure 6 the difference in transit time with collector voltage change with respect to  $V_c = 10 \text{ v}$  is plotted. From these results, in conjunction with ratios of  $r_{bb}$ ,  $C_c$  products derived from Figure 7,  $\tau_1 - \tau_2$  is plotted as a function of  $\ln(C_{c1}/C_{c2})$  in Figure 8. It is seen that a straight line relationship is obtained for collector voltages down to 3 v: this suggests that the assumed theory is applicable and the transistor approximates reasonably to the exponential model.

Also plotted in Figure 8 are points derived from common-base open-current output capacitance measurements. Neglecting stray capacitance between transistor leads, the output capacitance

$$C_{ob} = C_c + C_{cb}$$

and is the total collector depletion capacitance. Thus  $C_{ob}$  may be expected to behave with change of  $V_c$  in the same manner as does  $C_c$ ; this is seen to be the case, the latter points agreeing quite well with those derived from the  $r_{bb}$ ,  $C_c$  data.

From equation (12) the slope of the above straight line plot is  $L^2/D$ , giving for  $V_c = 5 \text{ v}$ ,

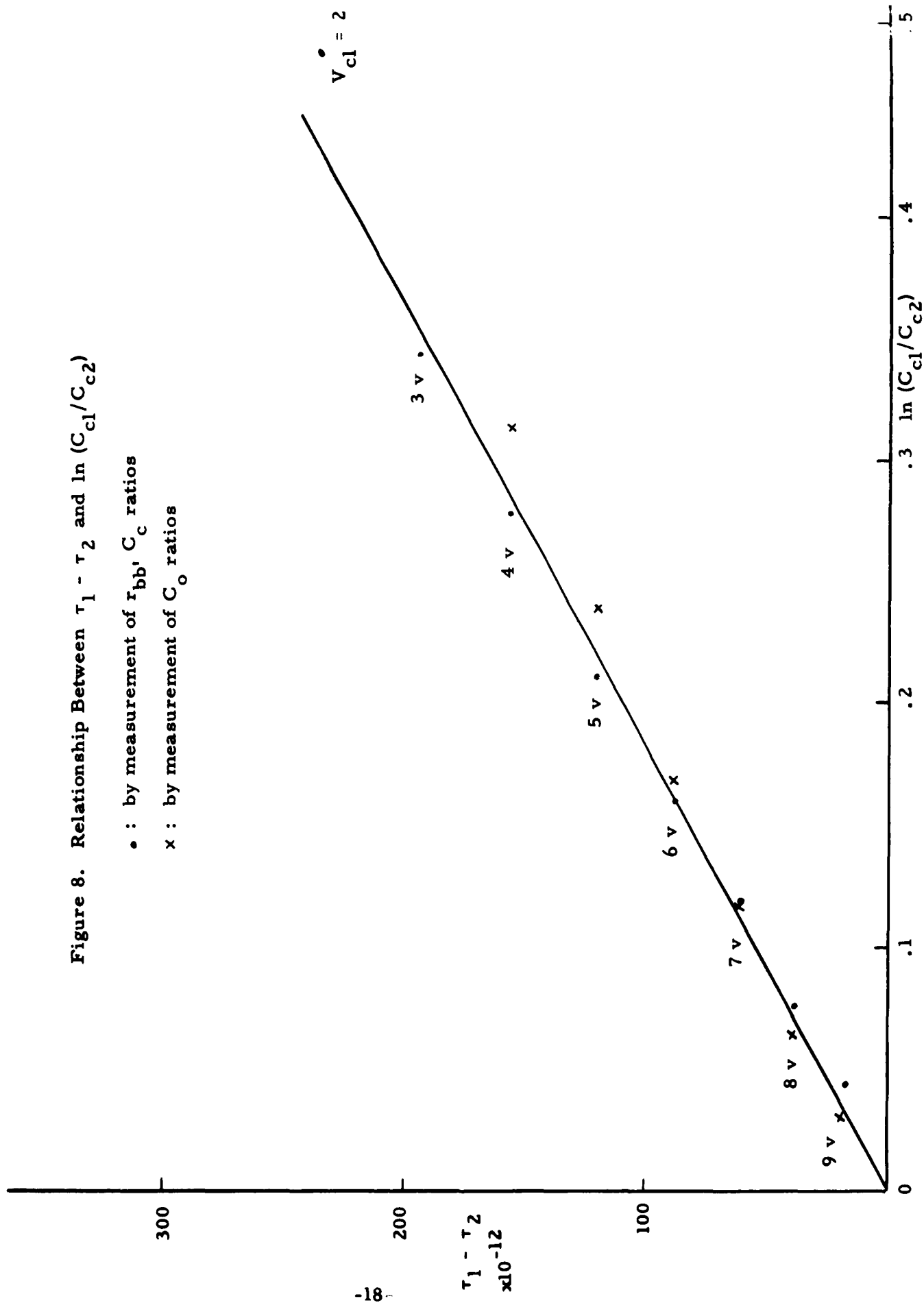
$$L = 1.3 \times 10^{-4} \text{ cm}$$

From equations (15) the values of the field factor and base width are

$$m = 5.35$$

$$w = 6.95 \times 10^{-4} \text{ cm.}$$

However, these values are accurate only if the ratio  $d/L$  is sufficiently large at the collector voltages considered for the approximation  $F \approx 1$  in equations (10) and (14) to be made.



#### IV.2 Other Measurements

In order to evaluate the ratio  $d/L$  and verify the above calculations it is necessary to determine the emitter area  $A_e$  and the collector capacitance  $C_c$  for the collector voltage concerned. Then

$$C_c = K A_e / d$$

Figure 9 gives measurements of  $1/C_{te}^2$  as a function of reverse emitter-base voltage. For voltages greater than 2 v a straight line relationship is exhibited, indicating approximate step junction behavior. From the slope of this straight line, according to equation (17)

$$N_1 A_e^2 = 8.84 \times 10^{10} \text{ cm}$$

The d.c. relationship between  $I_c$  and  $V_{eb}$ , plotted in Figure 10, is a straight line, the slope of which gives

$$\frac{A_e}{N_1} = .643 \times 10^{-20} \text{ cm}^5$$

It is noted from equation (18) that this last quantity is proportional to  $L$ , the above derived value of which has been used at this stage. If the value of  $L$  is later found to be in error owing to  $F \neq 1$ , the  $A_e/N_1$  ratio needs to be modified when solution by iteration is applied as discussed in Section II.3. Thus

$$A_e^3 = .569 \times 10^{-9} \text{ cm}^6$$

and

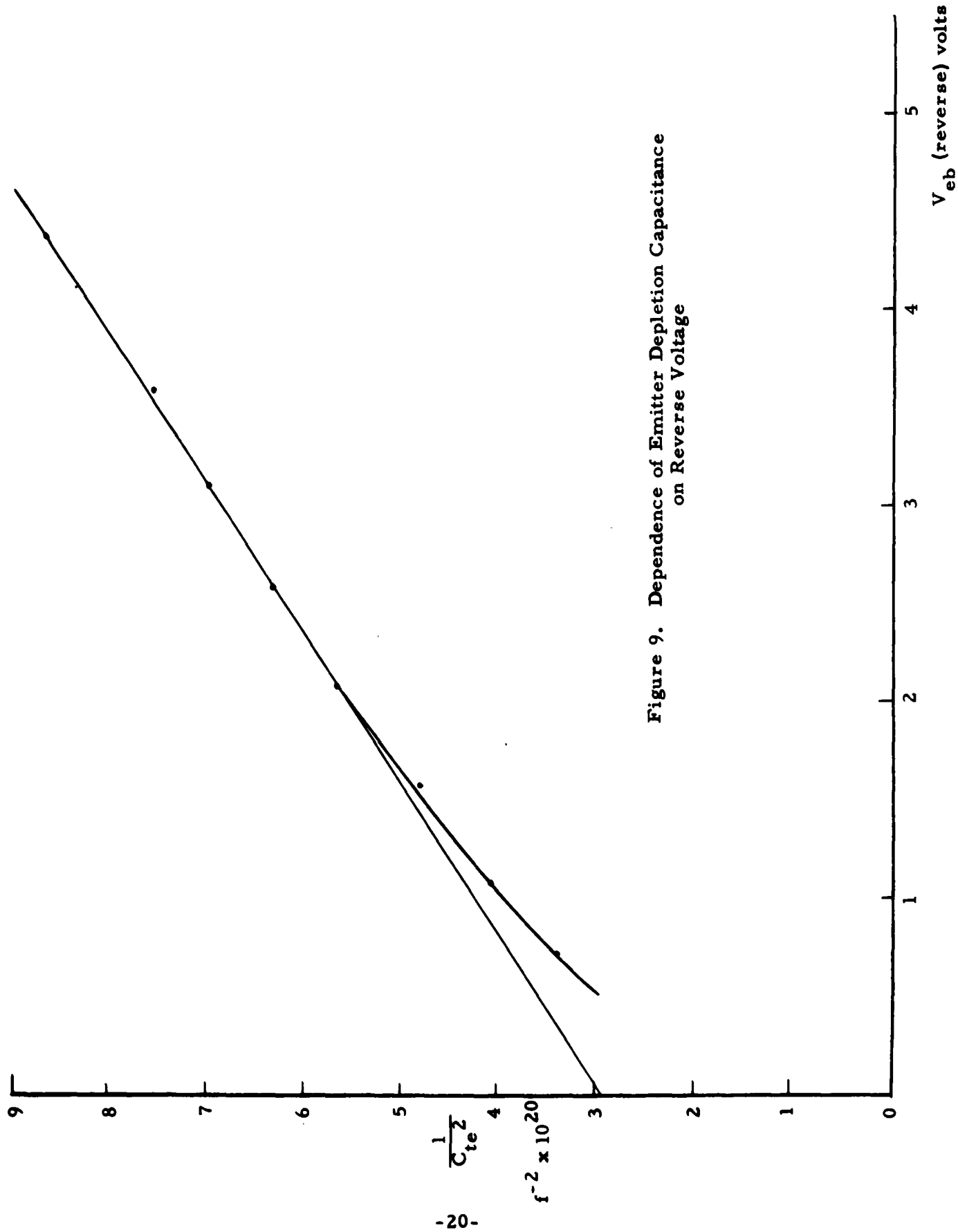
$$A_e = .83 \times 10^{-3} \text{ cm.}$$

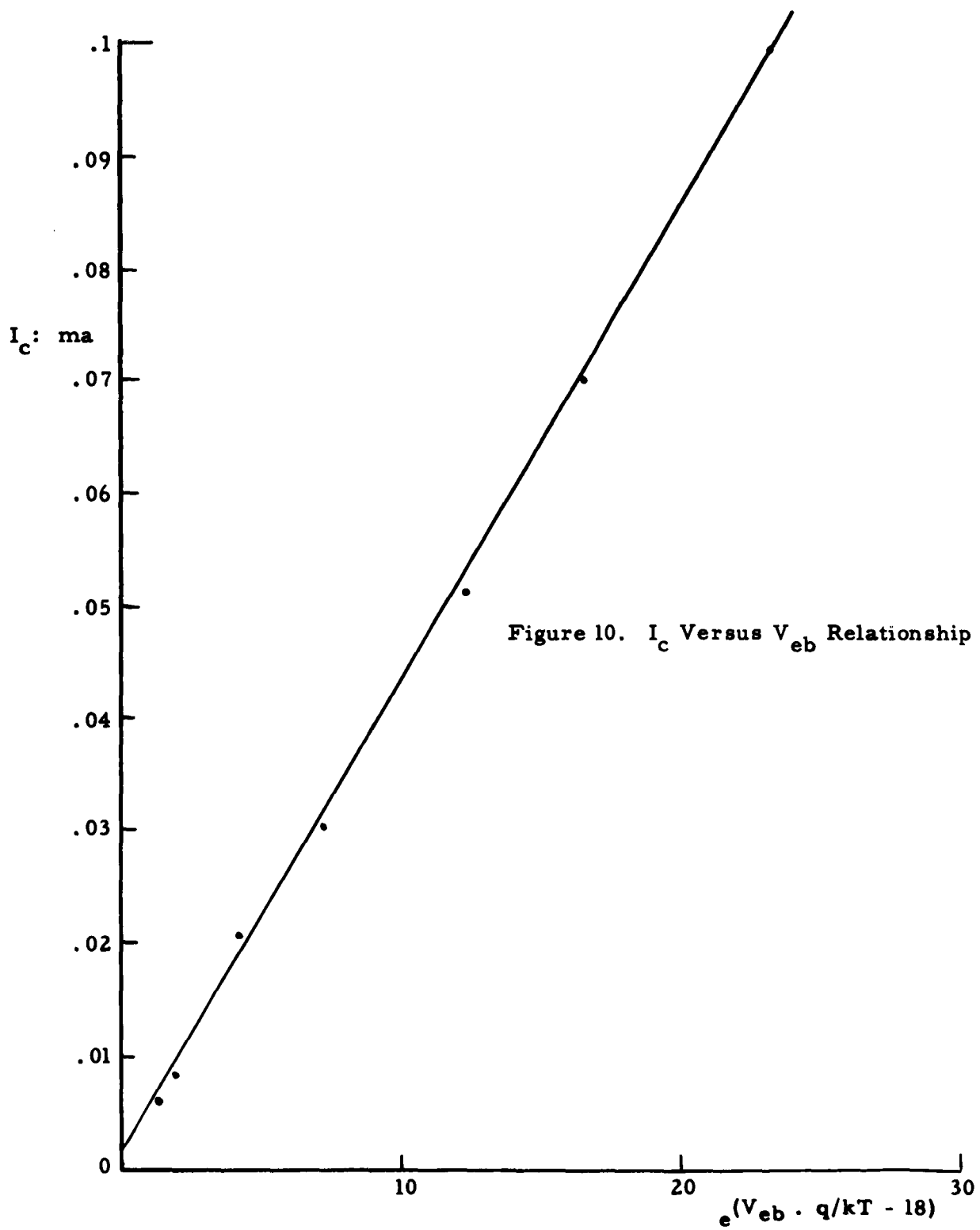
The  $r_{bb'}$ ,  $C_c$  product at  $V_c = 5$  v is seen from Figure 7 to be

$$r_{bb'} C_c = .57 \times 10^{-9} \text{ sec}$$

Thus it now remains to determine  $r_{bb'}$ , so that  $C_c$  and hence  $d$  may be calculated. The procedure of Section III.3, carried out at 1 mc/s with  $V_c = 5$  v and  $I_e = 0.2$  ma, yields

$$r_{bb'} = 625 - 476 = 149 \Omega$$





Details of this derivation are given in Appendix III.

$$\therefore C_c = 3.8 \text{ pF}$$

and

$$d = 2.33 \times 10^{-4}$$

$$\text{Hence } \frac{d}{L} = 1.79$$

and this value is insufficiently large for the approximation  $F \approx 1$  to be valid. Iteration must therefore be applied to determine the true value of  $L$ .

#### IV.3 Iteration Process

For the purpose of determining  $L$  by iteration, the collector voltages

$$V_{c1} = 3 \text{ v}$$

$$V_{c2} = 10 \text{ v}$$

were used for which, on the basis of  $L = 1.3 \times 10^{-4} \text{ cm}$  as above,

$$d_1 = 2.0 \times 10^{-4} \text{ cm}, \quad \frac{d_1}{L} = 1.54$$

$$d_2 = 2.87 \times 10^{-4} \text{ cm}, \quad \frac{d_2}{L} = 2.21$$

yielding

$$F = 1.13$$

Evaluating the modified value of  $L$  from equation (14) gives

$$L = 1.58 \times 10^{-4}$$

and results in change of  $A_e$  to

$$A_e = .883 \times 10^{-3} \text{ cm}^2$$

After recalculating  $d_1$  and  $d_2$  for this modified  $A_e$ ,

$$\left. \begin{array}{l} d_1/L = 1.35 \\ d_2/L = 1.93 \\ F = 1.156 \\ \text{and } L = 1.65 \times 10^{-4} \text{ cm} \end{array} \right\}$$

Finally, using this last L value,

$$\left. \begin{aligned} A_e &= .896 \times 10^{-3} \text{ cm} \\ d_1/L &= 1.31 \\ d_2/L &= 1.88 \\ F &= 1.16 \\ L &= 1.67 \times 10^{-4} \text{ cm} \end{aligned} \right\}$$

A further iteration results in negligible change in parameter values.

#### IV.4 Summary of Derived Parameter Values

Having determined values of L and d to satisfy equation (9), it is possible to calculate all parameters discussed in Section II. The final results of these calculations are given below:

$$\underline{V_c = 5 \text{ v}}$$

$$L = 1.67 \times 10^{-4} \text{ cm}$$

$$m = 3.64$$

$$w = 6.08 \times 10^{-4} \text{ cm}$$

$$A_e = 0.896 \times 10^{-3} \text{ cm}^2$$

$$D_e = 338 \times 10^{-4} \text{ cm (emitter diameter)}$$

$$d = 2.51 \times 10^{-4} \text{ cm}$$

$$d/L = 1.505$$

$$N_1 = 1.09 \times 10^{17} \text{ cm}^{-3}$$

$$N_2 = 1.47 \times 10^{15} \text{ cm}^{-3}$$

$$N_1/N_2 = 73.6$$

$$w_b = 7.18 \times 10^{-4} \text{ cm}$$

$$\tau = 2.36 \times 10^{-9} \text{ secs; } f_T = 67.5 \text{ mc/s}$$

$$C_{ob} = 22.2 \text{ pF}$$

$$C_c = 3.8 \text{ pF}$$

$$C_{cb} = 18.4 \text{ pF}$$

$$\begin{aligned}
C_{te} &= 128 \text{ pF}^+ \\
r_{bb'} C_c &= 0.57 \times 10^{-9} \text{ secs} \\
r_{bb'} &= 150 \Omega
\end{aligned}$$

## V. DISCUSSION

In the previous section, theory based on a device model with exponential base grading has been applied somewhat blindly to a double-diffused n-p-n silicon unit. The results derived may be regarded as referring to an equivalent exponential model of the actual transistor studied. Just how close the physical parameters obtained (e.g., base width, emitter area, depletion layer thickness) are to the corresponding quantities in the device can only be established by carrying out more detailed investigations.

Because of the diffused nature of the emitter junction (rather than the assumed step junction of Section II) it might be expected that marked divergence from the theoretical relationships of Section II would be observed during the course of the measurements. However, the relationship between  $\tau_1 - \tau_2$  and  $\ln C_{c1}/C_{c2}$  (Figure 8) is quite as predicted by theory, suggesting that deviations from exponential grading are not severe.

The plot of  $1/C_{te}^2$  against reverse  $V_e$  in Figure 9 indicates the gradual, rather than step nature of the emitter junction, the linear relationship being exhibited only for voltages greater than 2 v. Since for forward biasing of the emitter junction the depletion layer must, in view of the behavior of Figure 9, fall short of the region of highest impurity density in the base, the interpretation of the  $I_c \sim V_{eb}$  data of Figure 10 in terms of the expression of equation (18) is of uncertain significance. Again, provided that deviations from the assumed ideal device are not serious, use of this expression should presumably give the  $N_1$  value of an approximating exponential impurity density distribution.

It is interesting to compare derived physical parameters with device design data given by the manufacturer, as below:

---

<sup>+</sup>Derived from the slope  $(C_{te} + C_{ob}) r_d$  of the plot of  $\tau'$  against  $1/I_e$  in Figure 5.



	Device design value	From measurements
$D_e$	$375 \times 10^{-4} \text{ cm}$	$338 \times 10^{-4} \text{ cm}$
$N_1$	$1.4 \times 10^{17} \text{ cm}^{-3}$	$1.1 \times 10^{17} \text{ cm}^{-3}$
$N_2$	$2.5 \times 10^{15}$	$1.5 \times 10^{15} \text{ cm}^{-3}$

In view of the approximations made in applying the theory to the 2N696 unit, the agreement is remarkably good.

The extrinsic base resistance value listed in Section IV.4 would perhaps seem to be somewhat large for the type of transistor studied, and needs to be verified by other methods of measurement<sup>4</sup>. From the relative area of the emitter and collector as specified by the manufacturer (namely 1:4) a value of 5 pF would seem reasonable for  $C_c$ ; from the measured  $r_{bb'}$ ,  $C_c$  value of  $0.57 \times 10^{-9}$  secs, the corresponding  $r_{bb'}$  value would be 114  $\Omega$ . If this value is used in the calculations of Section IV, then  $L = 1.93 \times 10^{-4} \text{ cm}$ ,  $D_e = 346 \times 10^{-4} \text{ cm}$  and  $N_1 = 1.24 \times 10^{17} \text{ cm}^{-3}$ .

## VI. CONCLUSIONS

A possible approach to the derivation of physical parameters of drift transistors having a diffused collector junction has been presented on the basis of an exponentially graded base model. The measurements involved are all relatively simple and are carried out at quite low frequencies--i.e., frequencies of the order of  $f_\beta$ . No difficulty has been experienced in practice in performing the measurements involved with sufficient accuracy for their interpretation in analytic terms, provided that the theory is assumed valid for the device concerned.

Detailed studies have been made of a type 2N696 n-p-n silicon mesa unit. Although the base impurity density is known to depart appreciably from an exponential distribution, owing to the double-diffused process of fabrication, the results obtained appear to conform reasonably well to the exponential theory, certain of the derived physical parameters being quite close to the manufacturer's design values for the device.

More investigation is required before the true significance of physical parameters derived by the procedure presented in the report can be assessed. For some devices a complementary error function, or perhaps Gaussian, distribution of infinite density may be appropriate. The same general analytic procedure could be applied in such cases, though with greater complexity.

## APPENDIX I. DETAILS OF THE TRANSIT TIME BRIDGE

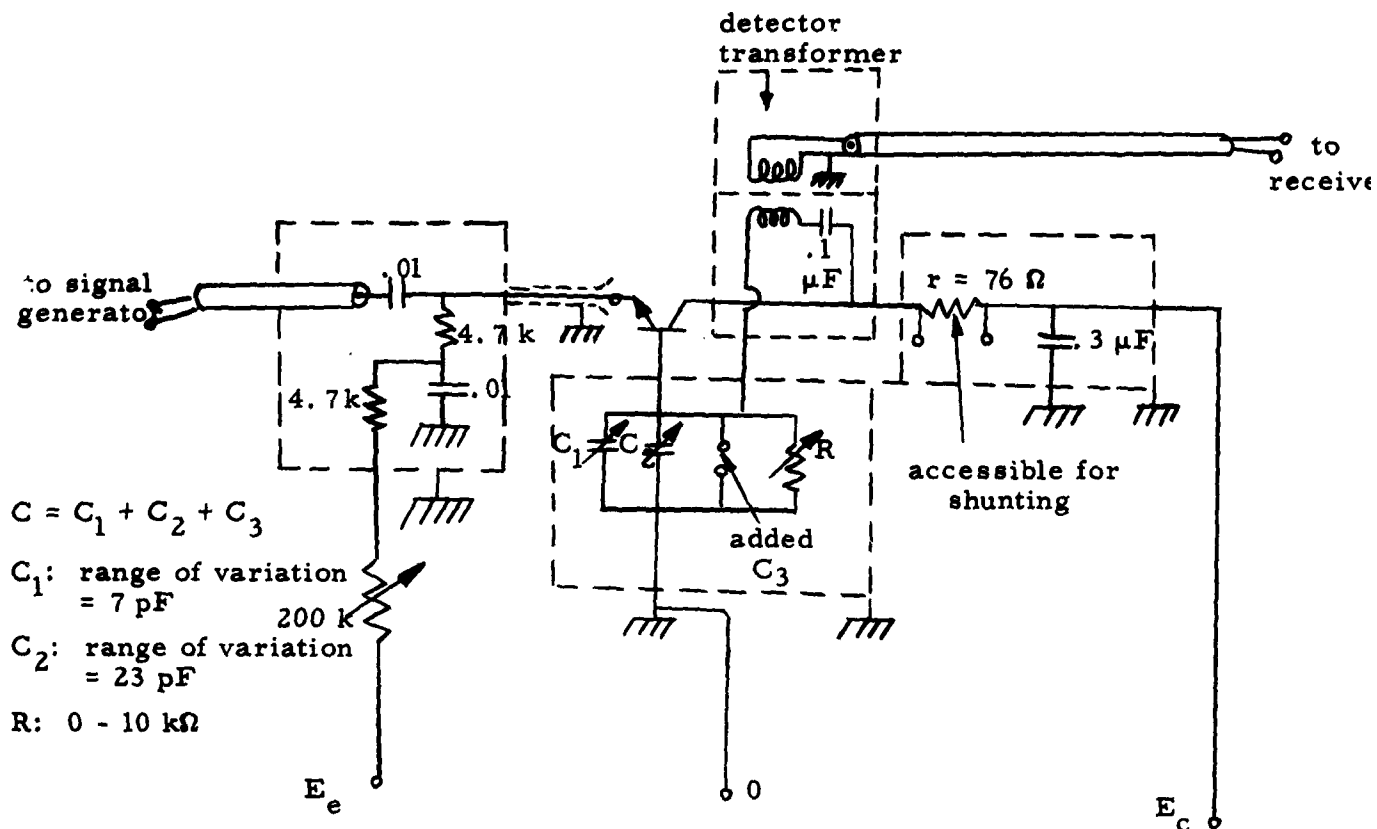
The circuit of the bridge used for the measurements of Section IV is given in Figure 11. For satisfactory operation a compact layout is necessary, care being taken to reduce stray effects and coupling between emitter, base and collector circuit meshes to a minimum. The arrangement adopted consisted of four screened compartments, within which were:

- base circuit elements  $C$ ,  $R$
- collector path through  $r$  to ground
- emitter excitation lead-in
- detector transformer.

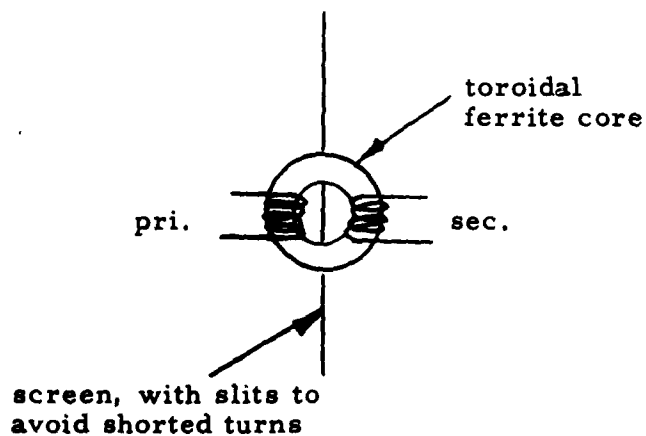
Interconnections between these screened boxes were kept as short as possible, with complete separation of emitter excitation and output detector transformer.

The variable capacitors  $C_1$ ,  $C_2$  were small vane-type with spindles and moving vanes grounded.  $R$  was an Allen-Bradley carbon track potentiometer with the moving contact grounded: this arrangement gave consistent calibrations of resistance over a long time period, while the stray capacitance was found to be  $\sim 2$  pF and constant over the full range of resistance (this capacitance was also constant over the frequency range 0.5 to 5 mc/s, for which the bridge was designed and operated).

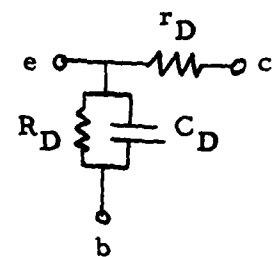
Particular care is necessary in the design of the detector transformer which converts out-of-balance voltage between collector and base to a voltage with respect to ground. The two windings need to be reasonably efficiently coupled magnetically yet screened from each other electrostatically. The construction adopted was to have the two halves of a  $1/2$ " D.



a) Circuit layout



b) Preferred design of detector transformer



c) "Transistor dummy" used for calibration of the bridge

Figure 11. Details of Bridge for Measurement of Effective Transit Time on  $\omega_T$

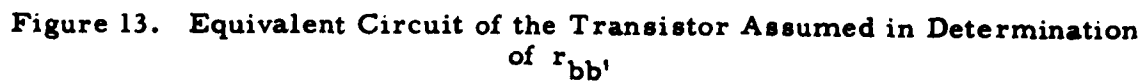
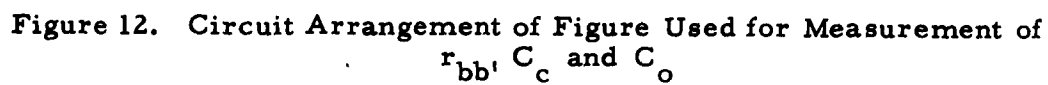
ferrite por-core assembly, containing the respective windings, separated by a thin (.006") grounded copper screening sheet (with appropriate slit): this gave excellent shielding but the distributed capacitance of the windings to ground was necessarily rather large (of the order of 10 pF). A better construction is as shown in Figure 11b, the two windings being on opposite extremes of a ferrite toroidal core and well separated from the screening sheet. A 1/2" D. toroid is very suitable for the purpose.

The bridge was constructed specifically for carrying out the measurements reported, but should have other features incorporated if employed generally for measurement of effective transit time  $\tau'$  or  $f_T$ . A single variable capacitor, possibly of range 10 - 60 pF is adequate provided other fixed capacitors can be switched in to give a sufficiently large range of the capacitance  $C$  (for example, capacitance steps of 50 pF up to 500 pF). While using the bridge it was necessary on occasions to reduce  $r$  by adding shunting resistors. This facility is best incorporated into the design of the bridge, means being provided for plugging or switching in shunting elements, without introducing undue lead strays. A useful minimum value of  $r$  is 10  $\Omega$ .

Bridge elements  $R$  and  $C$  were calibrated by direct admittance bridge measurements at the base terminal of the transistor socket, and by using the transit time bridge to measure the (known) elements  $R_D$ ,  $C_D$  of the "transistor dummy" shown in Figure 11c.

## APPENDIX II. DETAILS OF THE BRIDGE ARRANGEMENT FOR MEASUREMENT OF $r_{bb'}$ , $C_c$

Figure 12 gives the circuit details of the jig used for measurement of  $r_{bb'}$ ,  $C_c$ , in conjunction with the Wayne Kerr admittance bridge. The variable capacitor  $C$  was of moving vane type giving a range of 6 to 16 pF. Care was necessary to avoid stray capacitance effects associated with the circuit CR; for this reason the element  $C$  was mounted in a screening can. Calibration of  $C$  was carried out with the Wayne Kerr bridge by regarding the capacitor as a three-terminal element with respect to ground. Of the stray capacitances  $C_1$ ,  $C_2$  only the latter is significant in the operation of the bridge and the reactance of this is negligibly high in comparison with the resistance  $R$  for the frequencies concerned ( $\leq 5$  mc/s).



### APPENDIX III. DETERMINATION OF $r_{bb'}$ OF 2N696 SAMPLE STUDIED IN SECTION IV

Measurements made at 1 mc/s with  $V_c = 5$  v,  $I_e = -0.2$  ma gave

$$\tau' = 21.8 \times 10^{-9} \text{ sec}$$

$$\beta_o = 12$$

Assuming that in regard to the effects of  $C_{cb}$  on  $\tau'$ ,  $r_{bb'}$  may be neglected,

$$\tau' \approx \tau + r_d (C_{te} + C_c + C_{cb})$$

Thus, representing the transistor by the equivalent circuit of Figure 13,

$$C_c + C_{b'e} \approx \tau' r_d - C_{cb} = 150 \text{ pF}$$

$$r_{b'e} = r_d / (1 - \alpha_o) = 1695 \Omega$$

The impedance seen to the right of  $b'e$ , with collector started to emitter, may be written

$$r_1 + jx_1 = 1/y_{b'e}$$

where

$$r_1 = r_{b'e} / \left\{ 1 + r_{b'e}^2 \omega^2 (C_c + C_{b'e})^2 \right\}$$

$$= 476 \Omega$$

Now if the short-circuit base input admittance of the transistor in common emitter configuration is written

$$y_{11} = y_{11}' + j\omega C_{cb} = \frac{1}{R_{be}} + j\omega C_{be}$$

$$\text{and } 1/y_{11}' = r_2 + jx_2$$

$$\text{then } r_{bb'} \approx r_2 - r_1$$

Measurement of  $y_{11}$  gives

$$R_{be} = 1570 \Omega$$

$$C_{be} = 142.5 \text{ pF}$$

$$\therefore C_{b'e} = C_{be} - C_{cb} = 124.5 \text{ pF}$$

$$\text{and } r_2 = 625 \Omega$$

giving

$$r_{bb'} = 149 \Omega$$

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